Antennas’ Correlation Influence on the GMD-assisted MIMO Channels Performance

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Abstract: The use of multiple antennas in MIMO (multiple-input multiple-output) systems at both the transmit and receive sides produces the effect known as antennas correlation which impact the overall channel performance, throughput and bit-error rate (BER). The geometric mean decomposition (GMD) is a signal processing technique which can be used to process transmit and receive signals in MIMO channels. The GMD pre- and post-processing in conjunction with dirty-paper precoding shows some advantages over the popular singular value decomposition (SVD) technique which provides GMD-assisted MIMO systems a superior performance particularly when the channel is affected by antennas correlation. This paper analyses the impact of antennas correlation on the performance of GMD-assisted wireless MIMO channels highlighting the advantages over SVD-assisted ones.

1 INTRODUCTION

In the last decades researchers and engineers are facing the uphill to obtain higher transmission data rates and wider bandwidths required for the current and future high-speed services demanded by the industry and society, as video streaming, video-conference, massive data transfer, multi-user services, etc. In this context multiple-input multiple-output (MIMO) systems are playing a key role due to their capability to increase the channel throughput and performance compared with single-input single-output (SISO) systems (Foschini and Gans, 1998), (Ozgur et al., 2013). Due to their potential capabilities MIMO wireless communication systems have attracted a lot of attention from the research community. The use of spatial diversity in MIMO systems can considerably increase data rate and significantly improve the system robustness, reliability and coverage (Yang et al., 2011).

The use of multiple transmit and receive antennas causes effects which affect the channel performance. First, due to the multi-antenna configuration and the multi-path transmission inter-antennas interferences disturb the channel behaviour. MIMO systems benefit from multipath by using additional signal processing in order to improve the channel performance. Second, due to physical limitations the antennas at each side are really close compared to the wavelength and the correlation effect appears negatively impacting the MIMO channel performance (Janaswamy, 2002).

As stated above, in order to benefit the MIMO channels capabilities additional signal processing is required. The SVD is a popular technique widely used to improve MIMO channels performance (Haykin, 2002). Given perfect channel state information (PCSI) is available at both the transmit and receive link sides, the SVD is used to perform pre- and post-processing on the transmit and receive signals (respectively) to completely eliminate the existing inter-antennas interferences. As a result the MIMO channel is transformed into several parallel, independent and non-interfering single-input single-output (SISO) unequally weighted channels.

GMD-assisted signal processing seems to be an advantageous alternative to SVD-assisted signal processing in MIMO systems. The GMD can be used to process transmit and receive signals decomposing the MIMO channel into several SISO channels with
remaining inter-antennas interferences which must be eliminated by using additional signal processing (e.g., Tomlinson-Harashima pre-coding) to obtain the best channel performance. Along the investigation the Tomlinson-Harashima pre-coding is used in a frequency non-selective GMD-assisted MIMO system to perfectly cancel the inter-antenna interferences (Kinjo and Ohno, 2013).

In order to improve the SVD-assisted MIMO system performance, where the resulting SISO channels have different particular layer gains, bit and power allocation techniques based on the varying channel condition can be used (Zhou et al., 2005), which is synonymous of adaptive modulation. One of the main advantages of using the GMD is that the resulting independent layers have the same particular SISO channel gain coefficient (the geometric mean of the singular values), assuming that the inter-antenna interferences are perfectly eliminated by dirty-paper pre-coding. Hence, power allocation doesn’t make sense in GMD-assisted MIMO systems (a priori) avoiding the required computational overhead.

Antennas correlation is characterized by the antennas’ correlation coefficients which affect the channel matrix and hence its behaviour (Lee, 1973). The higher the antennas’ correlation the lower the channel scatter richness condition (required by MIMO systems to get a better behaviour) and the lower the overall performance. The correlation effect affects the geometric mean PDF which impacts the channel performance. The geometric mean PDF and the CCDF can be used to predict and optimize the MIMO channel performance by activating a proper number of layers which define different transmission modes configurations.

In (Benavente-Peces et al., 2013) the authors focused the investigation on the analysis of the singular values CCDF to evaluate the receiver-side antennas correlation effect on the channel performance and the outcomes of the appropriate antennas usage in a SVD-assisted MIMO system.

The novelty of this contribution is that a frequency non-selective MIMO link is studied independently of the antennas electrical properties to analyse the impact of antennas’ correlation on the performance of GMD-assisted MIMO systems. The effects on the channel matrix are highlighted and the resulting geometric mean PDF and CCDF are studied.

Additionally the benefits of having equal values of layer-specific weighting factors (i.e. gain coefficients) in GMD-based MIMO systems are remarked against the SVD-assisted ones using different number of active layers, highlighting the effect of correlation compared to classical uncorrelated channels. The geometric mean CCDF curves are used to analyse and predict the behaviour of the MIMO channel. The BER is computed for various active layers and the effect of antennas’ correlation is remarked to find the best transmission mode. A $4 \times 4$ MIMO system transmitting QAM signals along the active layers is considered as an example.

The remaining part of this paper is structured as follows. Section 1 shows the computation of the geometric mean of the channel matrix singular values. Section 3 describes the channel model for the GMD-assisted MIMO system, including the antennas’ correlation model. The analysed transmission modes are introduced in Section 4. Section 5 compares the GMD-assisted MIMO system versus the SVD-assisted one. In Section 6 the main results of the investigation are introduced including the geometric mean PDF and CCDF analysis, the antennas’ correlation effects and the considered transmission modes. Finally, Section 7 summarizes and highlights the main outcomes.

## 2 THE GEOMETRIC MEAN

The GMD with remaining interference elimination decomposes the MIMO channel into several independent SISO channels with equal performance. The main advantage that GMD-assisted MIMO systems present over the SVD-assisted ones is that those independent layers have the same gain coefficient which is the geometric mean of the singular values of the channel matrix. Hence, the additional computational load required to perform bit and power allocation to improve and optimize the MIMO channel performance is reduced. The geometric mean can be computed from the channel matrix singular values as:

$$\mu = \left( \prod_{i=1}^{L} \sqrt{\xi_i} \right)^{1/L},$$  

(1)

where $L$ is the number of activated layers (with $L \leq \min(n_T, n_R)$, $n_T$ and $n_R$ are the number of transmit and receive antennas respectively) and $\sqrt{\xi_i}$ (singular values) states for the positive square roots of the eigenvalues $\xi_i$ of $\mathbf{H} \cdot \mathbf{H}^H$, where $\mathbf{H}$ is the channel matrix and $(\cdot)^H$ is the hermitian operator.

## 3 CHANNEL MODEL

The MIMO channel can be described in general terms as

$$\mathbf{y} = \mathbf{H} \cdot \mathbf{c} + \mathbf{n}$$  

(2)
where \( \mathbf{c} \) is the \((n_T \times 1)\) transmit data vector, \( \mathbf{H} \) is the \((n_R \times n_T)\) channel matrix, \( \mathbf{n} \) is the \((n_R \times 1)\) noise vector at the receive antennas and \( \mathbf{y} \) is the \((n_R \times 1)\) receive data vector (with \( n_T \) the number of transmit antennas and \( n_R \) the number of receive antennas). By using the GMD the channel matrix can be decomposed as:

\[
\mathbf{H} = \mathbf{Q} \cdot \mathbf{R} \cdot \mathbf{P}^H \tag{3}
\]

where \( \mathbf{R} \) is an upper triangular matrix and \( \mathbf{Q} \) and \( \mathbf{P} \) are unitary matrices whose rows are orthonormal. Assuming the PCSI condition at both the transmit and receive sides, pre \((\mathbf{P})\) and post \((\mathbf{Q}^H)\) processing can be performed at the transmit and receive sides resulting in

\[
\tilde{\mathbf{y}} = \mathbf{R} \cdot \mathbf{c} + \mathbf{n}, \tag{4}
\]

where \( \mathbf{R} \) is an upper triangular matrix whose elements in the main diagonal equal the geometric mean of the singular values and the upper non-zero elements describe the remaining inter-antenna interferences, \( \mathbf{n} \) is the post-processed noise vector and \( \tilde{\mathbf{y}} \) is the resulting receive data vector. By using perfect interference cancellation (e.g. Tomlinson-Harshima pre-coding) the remaining interference can be removed and the channel can be finally described as

\[
\tilde{\mathbf{y}} = \mathbf{R} \tilde{\mathbf{c}} + \tilde{\mathbf{n}}, \tag{5}
\]

where \( \mathbf{R} \) is a diagonal matrix whose non-zero elements equal the geometric mean of the singular values. In order to improve the channel performance it is possible to select the appropriate number of active layers obtaining an extra gain in the geometric mean computation as only the largest singular values are considered (Jiang et al., 2005).

### 3.1 Singular Values vs. Geometric Mean

The SVD decomposes the channel matrix as \( \mathbf{H} = \mathbf{S} \cdot \mathbf{V} \cdot \mathbf{D}^H \), where \( \mathbf{V} \) is a diagonal matrix containing the singular values of \( \mathbf{H} \) in descending order, and \( \mathbf{S} \) and \( \mathbf{D} \) are unitary matrices. After pre- and post-processing the transmit and receive data vectors with matrices \( \mathbf{D} \) and \( \mathbf{S}^H \) respectively, the resulting receive data vector is given by \( \tilde{\mathbf{y}} = \mathbf{V} \cdot \mathbf{c} + \mathbf{n} \), where \( \mathbf{n} \) is the post-processed noise vector, described a system composed of several independent layers (SISO channels).

Figure 1 represents and compares the matrices \( \mathbf{V} \) (containing the singular values), \( \mathbf{R} \) (containing the geometric mean and remaining inter-antenna interferences) and \( \mathbf{R} \tilde{\mathbf{c}} \) (containing the geometric mean) for an exemplary \((4 \times 4)\) MIMO channel. Independently of the number of active layers the value of the singular values doesn’t change. On the other hand the value of the geometric mean depends on the number of active layers as shown in Fig. 1(b)-(f). For one active layer ((a) and (f)) the systems behave in the same way as the layer coefficient is the same in both cases. For four active layers the SVD-assisted MIMO system shows a weak layer which drops the overall system performance and the GMD-assisted one shows a higher performance. The cases concerning two and three active layers requires a more detailed analysis as different transmission modes can be considered and the final results depend on the real channel status.

### 3.2 Antennas’ Correlation

Antennas correlation is characterized by the correlation matrix which is composed of the correlation coefficients describing the dependencies of the multipath transmission. The correlation between antennas \( k \) and \( \ell \) is denoted as \( \rho_{k,\ell} \). Given a set of \( n_N \) antennas, the correlation matrix is a \((n_N \times n_N)\) one. As an example, the receiver side correlation matrix for a four receive antennas is given by

\[
\mathbf{R}_{RX}^{(4 \times 4)} = \begin{pmatrix}
1 & \rho_{12}^{(RX)} & \rho_{13}^{(RX)} & \rho_{14}^{(RX)} \\
\rho_{21}^{(RX)} & 1 & \rho_{23}^{(RX)} & \rho_{24}^{(RX)} \\
\rho_{31}^{(RX)} & \rho_{32}^{(RX)} & 1 & \rho_{34}^{(RX)} \\
\rho_{41}^{(RX)} & \rho_{42}^{(RX)} & \rho_{43}^{(RX)} & 1
\end{pmatrix}. \tag{6}
\]

Therein, the correlation coefficient \( \rho_{k,\ell}^{(RX)} \) de-
describes the receiver side correlation between the transmit antenna \( k \) and \( \ell \). It can be demonstrated that \( \rho_{kk}^{(\text{TX} \times \text{RX})} = \rho_{k\ell}^{(\text{TX} \times \text{RX})} \) and the matrix in (6) can be simplified. The transmit correlation matrix \( \mathbf{R}_{\text{TX}} \) can be described in a similar way. In the case of uncorrelated antennas, the off-diagonal elements are zero.

According to (Ahrens et al., 2013) the \((n_{\text{TX}} \times n_{\text{RX}})\) channel matrix \( \mathbf{H} \), which models a MIMO system affected by antennas' correlation can be obtained from the channel matrix of an uncorrelated MIMO system and the matrix modelling the antennas' correlation as:

\[
\text{vec}(\mathbf{H}) = \mathbf{R}_{\text{HH}}^{1/2} \cdot \text{vec}(\mathbf{H}) , \tag{7}
\]

where \( \mathbf{H} \) is a \((n_{\text{TX}} \times n_{\text{RX}})\) uncorrelated channel matrix with independent, identically distributed complex valued Rayleigh elements, \( \text{vec}(\cdot) \) is the vector operator which stacks the matrix \( \mathbf{H} \) into a vector column-wise and \( \mathbf{R}_{\text{HH}} \) is the correlation matrix which includes both the transmit and receive antennas' correlation. Taking into consideration the common assumption that the correlation between the various antennas composing the transmitter side array is independent from the correlation between the different antennas composing the receiver side array, the correlation matrix \( \mathbf{R}_{\text{HH}} \) can be described by the Kronecker product of the transmitter side correlation matrix \( \mathbf{R}_{\text{TX}} \) and the receiver side correlation matrix \( \mathbf{R}_{\text{RX}} \) as:

\[
\mathbf{R}_{\text{HH}} = \mathbf{R}_{\text{TX}} \otimes \mathbf{R}_{\text{RX}} . \tag{8}
\]

4 TRANSMISSION MODES

In this investigation a \(4 \times 4\) MIMO system with QAM modulation and a constant data rate with an overall throughput of 8 bits/s/Hz is considered. Hence, the possible transmission modes defined by the active layers are those shown in Table 1.

<table>
<thead>
<tr>
<th>Throughput</th>
<th>Layer 1</th>
<th>Layer 2</th>
<th>Layer 3</th>
<th>Layer 4</th>
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</thead>
<tbody>
<tr>
<td>8 bit/s/Hz</td>
<td>256</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>8 bit/s/Hz</td>
<td>64</td>
<td>4</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>8 bit/s/Hz</td>
<td>16</td>
<td>16</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>8 bit/s/Hz</td>
<td>16</td>
<td>4</td>
<td>4</td>
<td>0</td>
</tr>
<tr>
<td>8 bit/s/Hz</td>
<td>4</td>
<td>4</td>
<td>4</td>
<td>4</td>
</tr>
</tbody>
</table>

The different transmission modes are defined by the transmission of distinct QAM constellation sizes along the available (active) layers.

5 GEOMETRIC MEAN VS. SINGULAR VALUES

In order to improve the SVD-assisted MIMO systems performance bit and power allocation strategies can be used by selecting the appropriate number of active layers, the modulation order and the transmit power per layer in order to obtain the best performance, requiring additional computational load and transmission overhead. In GMD-assisted MIMO systems all the active layers have the same gain coefficient (the geometric mean) performing with the same quality, and hence power allocation is not required to improve the overall MIMO channel performance.

A concrete number of active layers can be selected to compute the geometric mean using (1) resulting in different MIMO channel performances. By selecting just one layer the geometric mean coincides with the singular value of that layer (the one with the largest value). Activating more layers with different singular values results in a geometric mean whose value is lower than the largest singular value. Even so the GMD-assisted MIMO performance is not lower than the SVD-assisted one given there are layers with low valued singular values. In fact GMD-assisted MIMO systems are (in general) more robust than SVD-assisted without requiring power allocation techniques. Nonetheless, the appropriate selection of the number of active layers (which is synonymous of bit allocation) can lead to the best performance, particularly under antennas' correlation effect.

Fig. 2 represents the geometric mean PDF for uncorrelated (solid lines) and correlated (dashed lines) \(4 \times 4\) GMD-assisted MIMO channels for a different number of active layers. The analysis reveals that the geometric mean decreases with the number of active layers, which is event more evident under antennas' correlation effect. As the considered number of active layers can be selected to compute the geometric mean using (1) resulting in different MIMO channel performances. By selecting just one layer the geometric mean coincides with the singular value of that layer (the one with the largest value). Activating more layers with different singular values results in a geometric mean whose value is lower than the largest singular value. Even so the GMD-assisted MIMO performance is not lower than the SVD-assisted one given there are layers with low valued singular values. In fact GMD-assisted MIMO systems are (in general) more robust than SVD-assisted without requiring power allocation techniques. Nonetheless, the appropriate selection of the number of active layers (which is synonymous of bit allocation) can lead to the best performance, particularly under antennas' correlation effect.

Fig. 2: Geometric mean PDF representation for uncorrelated (solid line) and correlated (dashed line) \(4 \times 4\) MIMO channels activating 1-4 layers.
of active layers increases lower valued singular values (weak layers) are used to compute the geometric mean through equation (1) obtaining a lower layer gain coefficient (geometric mean). In conclusion, due to antennas' correlation weak layers results in lower singular values and the geometric mean drops and wider spreads when various layers are activated.

A key different between SVD-assisted and GMD-assisted MIMO systems is that in the first ones reducing the number of active layers doesn't change the singular values and the individual layer gain isn’t altered. In contrast, in the second ones (i.e. GMD) selecting a lower number of active layers results in a larger geometric mean, which is the layer coefficient gain.

Fig. 3 depicts the PDF of the gain coefficients for a two active layers SVD-assisted MIMO system (with singular values \( \sqrt{\xi_i} \)) and GMD-assisted one (geometric mean \( \mu \)) for uncorrelated (solid lines) and correlated (dashed lines) cases. In the SVD-assisted MIMO channel the antennas' correlation effect favours the existence of strong (layer #1) and weak (layer #2) layers as the active layers singular values PDF curves become more spaced and smoothed. Hence power and bit allocation is required to optimize the performance. Conversely, in the GMD-assisted MIMO channel the geometric mean wider spreads with correlation but the mean value doesn’t significantly change (it slightly diminishes its value). In consequence it can be concluded that the GMD-assisted MIMO system behaves more robustly than the SVD-assisted one under the effect of the antennas' correlation. SVD-assisted MIMO systems are more sensitive to antennas' correlation. In these systems, as the correlation increases the strongest layer becomes indeed stronger (larger \( \sqrt{\xi_i} \)) and the weakest gets a lower singular value. Therein the overall MIMO channel performance drops due to the existence of low quality layers. In the GMD-assisted one, as the correlation increases the geometric mean decreases but in a reduced percentage and the overall performance slightly drops.

6 RESULTS

This section analyzes the results of the simulation of the GMD-assisted MIMO channel under different conditions. The goal is determining how the antennas' correlation affects the geometric mean of the singular values (layer gain coefficient) for different transmission modes and correlation indexes as well how the channel performance is affected. For convenience the correlation coefficients have been chosen to be the same for all the pairs of antennas.

6.1 Geometric Mean PDF and CCDF Analysis

In GMD-assisted MIMO systems (with pre-coding) bit- and power allocation make no sense as all the active layers perform with the same quality (BER) given the layers coefficients gain are the same. Nevertheless the selection of the appropriate number of active layers leads to different overall performances as the geometric mean differs. The larger the number of selected layers the lower the geometric mean and the lower the transmit QAM constellation size per layer at a given quality.

Fig. 4 shows the CCDF of the two largest singular values and the geometric mean of a \( 4 \times 4 \) MIMO channel when the two best layers are selected (two active layers). Under antennas' correlation effect the singular value CCDF curve of the strongest layer shifts right while the weak layer one shifts left. In consequence the overall SVD-assisted MIMO system performance diminishes. In the GMD-assisted one the geometric mean CCDF doesn't significantly vary with antennas' correlation and the overall channel performance is approximately the same. Then, the conclusion is drawn that the GMD-assisted MIMO system is more robust against the antennas' correlation effect than the SVD-assisted one.

The separation between the CCDF curves provides information to anticipate the system performance. When the CCDF curves are more spaced it seems to be more convenient the activation of a reduced number of layers to reach a better performance. This is because the weakest layer drops the computed geometric mean. Comparing the CCDF curves for uncorrelated and correlated MIMO channels, the last ones spread wider showing that for correlated MIMO channels choosing a reduced number of layers is more
appropriate. This effect is even larger in systems with antennas’ correlation.

Figures 5 to 8 depict the geometric mean PDF for a different number of active layers and distinct correlation indexes. For simplicity, in the investigation the same correlation coefficient is considered for each pair of antennas. Figure 5 represents the PDF when just one active layer is active for uncorrelated and correlated conditions, considering different correlation degrees ($\rho = \{0.0, 0.2, 0.4, 0.6\}$). In this case the geometric mean takes the value of the largest singular value (the stronger layer) of the resulting channel matrix. Increasing the correlation index augments the probability of having larger values, i.e., antennas’ correlation causes the strongest layer become even stronger because the singular value increases (and in this case the geometric mean).

The analysis of figures 6 to 8 gives different conclusions. Comparing the geometric mean PDF when 2, 3 and 4 layers are active for uncorrelated and correlated cases with a correlation index $\rho = 0.2$ (weak correlation) it can be observed that the geometric mean PDF doesn’t significantly change. As outcome, it can be concluded that GMD-assisted MIMO systems seem to be robust against antennas’ correlation. When two active layers are active the GMD-assisted MIMO seems to robustly behave under the antennas’ correlation effect. For the correlation indexes considered in our analysis the geometric mean PDF curves approximately centre in the same value. As the two weakest values are discarded the impact of the correlation index on the geometric mean is not quite remarkable and the system performance doesn’t noticeably change, except for the highest correlation index.

Figures 7 and 8 show the results when activating three and four layers respectively. Now the geometric mean value is more sensitive to correlation. This is due to the activation of the weakest layers (three and four) with low valued singular values which tend to take lower values as the correlation index increases. The first case shows to be more robust for low correlation indexes while the second one is more sensitive to correlation because the weakest layer (with the lowest singular value) is much more sensitive to the correlation effect, i.e., the singular value remarkably decreases with the increment of the correlation index.
6.2 The Effect of Correlation on the System Performance

Figures 9 to 13 show the effect of the antennas’ correlation on the performance of GMD-assisted MIMO systems for the transmission modes considered in Table 1. As reference, the BER for the equivalent SVD-assisted MIMO transmission mode is depicted. In the case in which just one active layer is active, the GMD- and SVD-assisted MIMO systems show the same behaviour. The analysis of figures 8 to 12, where a reduced number of available layers are activated, reveals that the GMD-assisted MIMO system performance increases with correlation (for low values). The reduction of the number of active layers discards weak layers in the computation of the geometric mean. Hence, the geometric mean is higher with a lower number of active layers. Under the antennas’ correlation effect, weak layers take indeed lower singular values and strong layers become stronger (higher singular values). As a result, the geometric mean takes higher values in correlated systems with a reduced number of active layers. This behaviour reverses when all layers are active. The increase in the correlation coefficient changes the described performance behaviour for an intermediate number of active layers.

6.3 Transmission Modes Comparison

Figures 14 to 16 represent the GMD-assisted MIMO channel performance (BER) for the analysed transmission modes described in Table 1 for different antennas’ correlation degrees. Power allocation is not considered in the different transmission modes and the same power is transmitted along the active layers. Figure 14 compares the performances obtained by the GMD-assisted MIMO system for the different transmission modes when affected by antennas’ correlation with a factor \( \rho = 0.2 \) (weak correlation). The results reveal that the transmission mode 16-16-0-0 (with two active layers) is the one showing the best performance.

The increase in the correlation coefficient affects the MIMO performance as described above. Figure 15 represents the performance for the various transmission modes.
mission modes and a correlation factor \( \rho = 0.4 \) (moderate). Now the effect of the correlation is noticed. The best performance is obtained with the transmission mode 256-0-0-0, i.e., activating just one layer. Finally, figure 16 depicts the BER performance for a correlation factor \( \rho = 0.6 \) (strong). Now the antennas’ correlation effect is noticeable and the transmission mode with the best performance is (TM 256-0-0-0), i.e., the case in which just one layer is active.

The analysis of the three figures provides clear conclusions. The transmission mode 4-4-4-4 with four active layers shows the worst performance in all the cases. This is because in the computation of the geometric mean we are considering the layer fourth, the one with the lowest singular value. Moreover, the correlation effect favours the appearance of weak layers which negatively affects the resulting geometric mean of the singular values. Furthermore, the correlation also favours the appearance of very strong layers. In this case, the lower the number of active layers the higher the resulting geometric mean. This is because the transmission mode 256-0-0-0 shows the best performance for moderate and strong correlation.

A key point in this discussion is the comparison between transmission mode 16-4-4-0 (with three active layers) and transmission modes 64-4-0-0 and 16-16-0-0 (with two active layers). For moderate correlation transmission mode 16-4-4-0 performs better than 64-4-0-0. As correlation increases the third active layer shows a lower singular value and the geometric mean drops resulting in a worse performance (as shown for \( \rho =0.4 \) and \( \rho =0.6 \)). Furthermore, the transmission mode 16-16-0-0 show a better performance than 64-4-0-0 (in this example). The equal distribution of bits along the active layers seems to be better than the unequal distribution given by transmission mode 64-4-0-0. Nevertheless this is not a general rule and depends on the resulting geometric mean.

7 CONCLUSIONS

This paper analyses the performance of exemplary 4 × 4 GMD-assisted MIMO systems affected by antennas’ correlation focusing on the geometric mean.
The activation a different number of layers results in distinct transmission modes which show different performances as shown in the results. In order to minimize the overall BER the same constellation size as well as the same transmit power per layer should be used. Although individual layers in GMD-assisted MIMO systems perform in the same way as the gain coefficient is the same, the appropriate usage of different constellations per layer can improve the overall MIMO channel performance.

Activating a larger number of layers takes into account weak layers. In consequence, due to the low valued singular values of weak layers the computed geometric mean diminishes and the GMD-assisted MIMO system performance drops. This outcome is much more remarkable as the antennas’ correlation increases. At the opposite side, activating just one layer leads to the largest geometric mean value. Nevertheless the best performance is not reached because a high order constellation is transmitted. An intermediate number of active layers seems to be the most appropriate solution which depends on the particular correlation index.

REFERENCES


