Evaluation of wave loads on a new type of perforated caisson

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A new type of perforated breakwater has been tested combining the advantages of cylindrical geometry with stepped wave energy dissipation. Thus, the new type of caisson implies a significant reduction of maximum wave forces, as well as loads transmitted to the foundation in comparison with conventional vertical breakwater and other types of perforated caissons. Starting from a brief description of the model and test results, this paper describes the development of a methodology for the estimation of maximum wave loads on this type of breakwater, in order to become a generalisable tool for predesign purposes. Construction and installation constraints of this new type of caisson are also assessed. These need to be taken into account in order to keep some advantages from the proposed design, while noting the key factors from a practical point of view.

Notation

- \( A \): orbital amplitude of the wave movement
- \( B \): chamber width
- \( B_{eq} \): width of rubble berm, averaged over height of berm \( h_b \)
- \( B^* \): relative berm width (McConnell)
- \( B/L \): relative chamber width
- \( C_d \): drag coefficient
- \( C_e \): effective drag coefficient
- \( C_m \): inertia coefficient, \( C_m = 1 + C_{in} \)
- \( C_{in} \): added mass coefficient
- \( D, D_{front} \): cylinder’s diameter in the front wall
- \( d \): water depth over berm in front of the caisson
- \( d' \): water depth inside the caisson chamber
- \( E' \): incident wave energy per unit length
- \( F_{cal} \): estimated horizontal wave force according to the predictive model for this new type of caisson
- \( F_{conv} \): peak horizontal wave force according to the vertical wall
- \( F_i \): inertia force
- \( F_{inn} \): peak horizontal wave loads in the present innovative caisson
- \( F_R \): Froude number
- \( F_{slid} \): sliding safety factor
- \( F_{h+ve} \): horizontal wave forces on the front cylinder
- \( F_{h-ve} \): seaward wave forces on the front cylinder
- \( F_{2h+ve} \): horizontal wave forces on the rear cylinder
- \( F_{2h-ve} \): seaward wave forces on the rear cylinder
- \( G \): width of the gap between adjoining cylinders in the front wall
- \( g \): gravity acceleration (9.81 m/s\(^2\))
- \( H \) or \( H_{reg} \): regular wave height
- \( H_b \): wave height at breaking
- \( H_D \): design wave height
- \( H_i \): incident wave height
- \( H_{max} \): maximum regular wave height tested
- \( H_s \): significant wave height
- \( H^* \): relative wave height
- \( H' \): arithmetic mean wave height
- \( H/L \): wave steepness
- \( H_{1/250} \): mean of the 4% largest wave heights
1. Introduction

Perforated caissons, as well as other innovative alternatives to classical vertical wall breakwaters, have been developed under different approaches over the last decades. Usually new structure types pursue reduction in wave forces, which implies, as a major advantage, lower loads transmitted to foundations. In addition, short-duration impact loads have been demonstrated in some cases as the key factor leading to breakwater failures. This fact, among others, was dealt with in the report of the International Navigation Association (Pianc) working group 28 (Pianc, 2003), where four breakwater failures (within a set of 14 existing breakwaters under study) were reported due to smaller waves than design waves.

The decrease in wave reflection is another objective, in this case for functional reasons, strongly linked with the performance of the breakwater against wave action.

Conceptually, the first endeavour is focused on the evaluation of the reduction in pressures transmitted to the foundation for a new type of caisson. This reduction is driven by two main contributions: the structure’s dead weight and limited maximum wave loads.

Two main factors may be highlighted as the key design features of this new type of caisson: cylindrical geometry in the perforated front wall and a single open chamber. Derived from these features are the advantages regarding hydraulic performance: reduction in maximum wave pressures in the front wall, stepped incident wave energy dissipation (dividing the impact on the structure between front and rear walls, lagging them in time) and wave energy dissipation due to turbulence within the chamber itself.

In this paper, first, reductions in loads transmitted to the foundation are briefly summarised according to specific physical model tests. Then, the development of a new model for wave load predictions is presented. For this purpose, the results from previous reference works are taken as a starting point, in order to focus on those descriptive variables that may lead to more relevant conclusions. Potential scale effects are also discussed and evaluated and, finally, major constructive and installation constraints are identified. Thus, further minor design adaptations could be adopted to enhance the practical applicability of this new breakwater type for different locations.

2. Brief description of the new type of caisson

The work is based on a physical model test campaign which Dragados, S.A., the new product’s owner, undertook in the Barcelona Applied Hydrodynamics Institute’s (INHA) laboratory in co-operation with the Universidad Politécnica de Madrid, the Universitat Politècnica de Cataluña and the International Centre for Numerical Engineering Methods (CIMNE).

Figure 1. Conceptual picture of the caisson
The innovative type of caisson (Figure 1) consists of two vertical, parallel, cylinder walls separated from each other, shaping a chamber between them.

As with other types of perforated caissons, the front wall is partially porous. The front cylinders are separated so that some of the incident wave energy can pass through the gaps. This wave energy is then dissipated both in the caisson chamber and on the rear wall, which is also formed by separated vertical cylinders. The rear wall may likewise be discontinuous (as the front wall) or continuous (with plane walls connecting adjoining cylinders), as is the case in the present research.

Both walls are made of reinforced hollow cylinders, which are filled with granular materials (sand or gravel). The thickness of the cylinders’ walls may range from 0·40 to 0·45 m. Indeed, the thickness may be conditioned by the filling process of the cylinders, as will be discussed later when assessing the construction constraints. The cylinders are closed at the bottom and top ends with 2·00 m thick mass concrete plugs.

Every cylinder is braced at the top and bottom against the cylinder of the opposite wall. So the distance between centre lines of adjoining cylinders must therefore be the same in both walls. In addition, all the cylinders in the front wall must be braced at top and bottom. The top and bottom tie beams connecting the cylinders can be prefabricated (presressed concrete beams) but they may also be constructed and connected to cylinders during the caisson fabrication.

Caissons must have a modular design to be manufactured with the current construction techniques. Specifically, the caisson can be adapted to be built in a floating dock with a sliding formwork technique. Caissons with seven front and seven rear cylinders have been constructed under such conditions, with a distance of 7 m between the centres of adjacent cylinders in both walls, so the total length of the caisson is close to 49 m, since the diameter of the back cylinders is 6·25 m. This is compatible with the capacities of the majority of current floating docks. However, the caisson width, which is a major parameter in hydraulic performance since it defines the dimension of the chamber, is also highly constrained by the usual capacities of floating docks, and it has been taken into account in the model tested.

This is a complex system and so effort should not be focused on seeking an absolute optimum but on a validation of the new type, identifying the most influential variables. For this purpose, initial values were adopted within the usual ranges for key geometrical parameters according to scientific literature, mainly the works by Takahashi (2002) and Takahashi et al. (1991, 1994) and those referred to by Oumeraci et al. (1998) in the European Union ‘Proverbs’ project. Owing to the specific design based on cylindrical elements, some concepts will be specifically adapted. First the ‘coefficient of cylinder density’ \( \Phi \) of the front perforated wall can be defined as follows:

\[
\Phi = \frac{n_{cil}D}{(n_{cil}D) + (n_{exp}G)}
\]

where \( D \) is the cylinder’s diameter in the front wall, \( G \) is the width of the gap between adjoining cylinders in the front wall, \( n_{cil} \) is the number of cylinders in the front wall and \( n_{exp} \) is the number of gaps in the front wall. This factor is equivalent to the wall density concept, complementary of wall porosity \( n \) for perforated caissons. So for the sake of clarity, \( \Phi \) is used here instead of \((1-n)\), noting also that it refers to cylindrical and not plane geometry.

Another reason for the use of this density concept \( \Phi \) instead of the classical porosity is due to the evaluation of the blockage effect of the structure as it is dealt with by Chakrabarti (1994) in the discussion of scale effects in the Appendix at the end of the paper, in order to be consistent with other existing studies on the influence of a group of vertical cylinders.

Thus, the front wall was tested with three different cylinder diameters: 5·00, 4·70 and 4·50 m, in order to evaluate the influence of the gaps’ width on wave loads. Thus, \( \Phi \), defined according to Equation 1, ranged from 0·64 to 0·71 (i.e. equivalent values from 0·36 to 0·29 of the porosity concept for perforated vertical walls).

The back cylinders were predesigned with a diameter of 6·25 m, with 0·75 m wide vertical walls connecting adjoining cylinders. The chamber width \( B \) has ranged from 14·98 to 15·32 m, performing as a large space for wave energy dissipation. There are two main reasons for this chamber width range. First, it is compatible with the usual floating docks’ capacities for the construction of caissons; second, the rate \( B/L \) (relative chamber width) is in the range 0·10 < \( B/L \) < 0·20. Values of \( B/L \) close to 0·20 have been proved to be around the optimum for reducing wave loads and reflection coefficient in front of the structure in other tests – both with regular and irregular waves – for perforated caissons with single- or multi-chamber systems. Ijima et al. (1976) have shown a minimum of reflection coefficient when \( B/L \) is close to 0·20, as was also proved by Sawaragi and Iwata (1978) and by Tanimoto and Yoshimoto (1982). Allsop (1995) evaluated the performance of the reflection coefficient in a wide range of \( B/L \), for porosities ranging from 14 to 28%, a single chamber and a solid back wall, resulting in the lowest reflection coefficients at \( B/L = 0·25 \), while the highest reflections are expected at \( B/L = 0·50 \). Bergmann and Oumeraci (2000) compared both reflection coefficients and loads transmitted to the structure for single- and multi-chamber caissons and different wall porosities, finding...
that multi-chamber caissons are more efficient at reducing wave reflection than single-chamber caissons for a wider range of wave periods, and minimum values of reflection coefficient and wave loads when $BL$ is close to 0.20. Zhu and Chwang (2001) developed physical model tests with regular waves in order to validate their analytical models, and the results showed a minimum value of reflection coefficient for $BL$ close to 0.20, increasing as the immersion of the front wall decreased. Kirca and Kabdasli (2009) tested a perforated caisson with two chambers divided by a horizontal diaphragm, with different porosities of the front wall and with regular and irregular wave series, showing that this type of caisson can lead to a reduction in wave forces up to 30–40% when $0.20 < BL < 0.30$. The aforementioned are listed just to provide some relevant examples. On the other hand, cases where $BL$ values are close to 0.10 also need evaluation because they may be bound by constructive capacity constraints.

The caisson’s foundation level was −20.00 m, with sea water level (SWL) at ±0.00 m; it was placed on a 2.00 m thick embankment. The embankment extension in front of the caisson was 6.00 m wide while the seabed level was modelled at −22.00 m.

Finally, the crown wall is located above the rear wall being the crest freeboard +8.40 m, while the top of the front cylinders is at +3.00 m.

3. Test methods

3.1 General description

The instrumentation system was designed to record not only peak spatial pressure distributions on the different surfaces of the structure but also load time and duration distributions (impact rise time and load duration). Therefore, extreme care was taken in measuring phase lags between forces (horizontal and vertical).

Tests were undertaken at the INHA’s wave flume (two dimensional) in Barcelona, applying the Froude similarity for a scale of 1:25. The flume bathymetry had a single slope of 1:67. In the following, inputs and results are presented in prototype terms unless otherwise stated.

Tests were performed in a 52 m long, 1.8 m wide, 2 m deep flume equipped with a piston-type wave generator. During the tests, water depth at the paddle was 1.50 and 0.88 m in front of the breakwater’s model (so water depth is 22 m for the prototype). The maximum non-breaking wave that can be generated is 0.60 m at model scale (15.00 m at prototype scale) for the range of tested wave periods. Wave absorption systems were placed at both the rear of the actuator and at the front of the flume. The Aways software (Aalborg University) was used both for wave generation and real-time absorption of reflected waves.

The model was instrumented with 24 pressure sensors fitted at different points on the structure, apart from two load cells at the base of two of the cylinders (one front and one back) facing each other. These cells are able to measure horizontal and vertical forces while pressure sensors are used to determine wave pressure distributions along the cylinders. The overtopping was measured by installing collector chutes behind the rear wall (Figures 2 and 3).

3.2 Test wave conditions

Waves generated were regular in order to be able to analyse parametrically the hydraulic performance.

For the first stage ($D_{float} = 5.00$ m), a total of seven regular wave heights ($H$) were tested between 4.0 and 11.6 m in a prototype (0.16–0.46 m in a model) and periods between 7.5 and 12.5 s (1.5–2.5 s in a model). In the second phase ($D_{float} = 4.50$ and
4.70 m), a total of five wave heights were tested between 6 and 11.5 m in a prototype (between 0.24 and 0.46 m in a model), and periods between 7.5 and 12.5 s in a prototype (1.5 – 2.5 s in a model).

Wave conditions were chosen to avoid plunging breaker conditions, as shown in Table 1. Thus, it is possible to assess the performance of the new solution compared with a conventional vertical breakwater in the same location with classical models: Goda (1985) for positive forces and McConnell et al. (1999) or Sainflou (1928) for negative (seaward) forces.

That is, the wave conditions tested would correspond to quasi-static wave loads since regular wave conditions have been modelled. Accordingly, hereafter, predictive models based on quasi-static wave loads on vertical breakwaters are used for comparison. In any case, there were a number of series with $H_r/h_s \geq 0.50$, and indeed short-duration impact loads were recorded in some cases.

### 4. Test results

#### 4.1 Overtopping results

As described by Pullen et al. in the Eurotop manual (EurOtop, 2007), wave overtopping is a dynamic, discontinuous process and it is primarily governed by individual wave heights relative to the crest freeboard of the seawall.

Since these tests have been carried out with regular waves, and commonly accepted overtopping models are developed from random waves, it is necessary to ‘translate’ the results from the regular pattern to the equivalent situation with irregular waves.

When a set of laboratory records on the rate of overtopping $q_0$ by regular waves with various combinations of heights and periods is available, an approximate value of the mean rate of random wave overtopping ($q$) can be estimated with the following formula by Goda (2010).

\[
q \approx \int_0^\infty q_0(H|T)p(H)dH
\]

where $q_0(H|T)$ is the overtopping rate by regular waves with height $H$ and period $T$; $p(H)$ is the probability density function of wave height.

As regards the probability density function, the Rayleigh distribution can be used. According to Goda (2010), Equation 2 gives reasonably good approximations compared with the results of direct measurements with irregular waves in the laboratory for vertical walls in intermediate and deep waters, resulting in every case that $q > q_0$, as was first evaluated in experimental tests by Paape (1960). This approach is only valid when the influence of wave period between different situations is small or negligible.

In Figure 4, tests’ overtopping results are shown for two scenarios of the front cylinder diameters. These overtopping values have been modified according to Equation 2 in order to show the equivalent values for random waves. Furthermore, the results should be considered for estimation purposes only since the different wave heights were tested with different periods, and therefore the equivalence may not be very accurate.

The initial crest freeboard relative to SWL was +8.40 m. The overtopping rates have been compared with those predicted.

### Table 1. Type of wave loadings during the tests

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Parameter definition</th>
<th>Value range tested</th>
<th>Situation according to ‘Proverbs’</th>
<th>Type of wave loading in vertical breakwaters according to ‘Proverbs’</th>
</tr>
</thead>
<tbody>
<tr>
<td>Relative berm height</td>
<td>$h^* = h_b/h_s$</td>
<td>0:09</td>
<td>$h^* &lt; 0.30$</td>
<td>Vertical breakwater</td>
</tr>
<tr>
<td>Relative wave height</td>
<td>$H^* = H_s/h_s$</td>
<td>0:18 $\leq H^* \leq 0.56$</td>
<td>0:18 $\leq H^* \leq 0.35$: small waves</td>
<td>Quasi-breakwater</td>
</tr>
<tr>
<td>Relative berm width</td>
<td>$B^* = B_{eq}/L$</td>
<td>0:05 $\leq B^* \leq 0.09$</td>
<td>0:35 $\leq H^* \leq 0.56$: large waves</td>
<td>Impact loads</td>
</tr>
</tbody>
</table>

Figure 4. Overtopping comparison. Crest freeboard relative to SWL +8.40 m.
by Franco’s model (Franco & Franco, 1999) for vertical wall breakwaters and the same crest level.

For the equivalence of wave heights, \( H_{\text{reg}} = H = H' \) was adopted (in which \( H \) is the regular wave height in tests; \( H' \) is the arithmetic mean wave height of the storm) and the usual relations between representative wave heights according to the Rayleigh distribution

3. \( H_s \approx 1.60H' \)

4. \( H_{\text{max}} \approx 1.80H_s \)

Thus, for the estimation of \( q \) in Equation 2, the overtopping records for every wave height tested (\( q_0 \)) were used as well as the probability density according to the Rayleigh distribution, that is the values of \( p(H/H_{\text{reg}}) \), while for Franco’s formula \( H_s \) values have been taken according to Equation 3.

Other equivalences could be used for this comparison, for example \( H_{\text{reg}} = H_s \) or \( H_{\text{reg}} = H_{\text{max}} \). In these cases, the resulting values of \( q \) would be modified both in the estimation of equivalent random wave overtopping for this perforated caisson and also for the vertical type because the input values of \( H_s \) for Franco’s formula should be modified accordingly. So these results should be considered for relative comparison purposes only rather than for an accurate quantitative evaluation of overtopping rates (Figure 4).

To obtain random waves’ overtopping rates of the same order of magnitude according to the procedure described above, the crown wall height for vertical breakwaters should be around +15 m level.

4.2 Comparative summary of wave loads and bearing pressures transmitted to the foundation

The following results were drawn up on the basis of measuring wave forces at design critical instants, which correspond with the maximum horizontal wave forces both in the wave direction \( (F_{h+ve}) \) and the seaward direction \( (F_{h-ve}) \). Similarly, maximum overturning moments in both directions are shown. Although maximum horizontal forces and maximum moments do not happen exactly at the same time, this assumption is not far from the reality. Thus, adopting these values simultaneously keeps the calculation on the side of safety, since this involves maximum eccentricity and, thus, pressures transmitted to the foundation.

There are other critical instants regarding structural viability of the caisson, which are those with maximum values of \( F_{h+ve} + F_{h-ve} \) and vice versa, corresponding to maximum compressive and tensile stresses in the top connection beams between front and rear cylinders. This issue is not addressed in this paper since it has no geotechnical implications.

It is worth mentioning that horizontal wave loads and moments were measured by the load cells fitted, respectively, at the base of the front and rear central cylinders and checked by the approximate integration of records of pressure sensors along the cylinders at every instant.

The worst configuration regarding maximum wave forces and moments was the case with \( D_{\text{max}} = 4.50 \) and 2.50 m gaps between adjacent cylinders. Additionally, wave forces were recorded in three different configurations regarding the front tie beam at the top of the cylinders: at +3·00 m, at −6·00 m and with no front tie beam. The influence of this element of the design is considered later in Equation 7.

An approximate comparison with a conventional caisson is made, using Goda (1985) and Saintfle (1928) models for positive and seaward forces, respectively.

The same caisson foundation level (−20·00 m), embankment extension in front of the structure (6·00 m) and seabed level (−22·00 m) are supposed for comparison of both types. For the vertical type, a 26·00 m wide caisson is adopted with crown wall top at +15·00 m, which has been proved as the freeboard for similar random wave overtopping rates.

Figures 5–8 correspond to the aforementioned design critical instants (Tables 2 and 3).

4.3 What arises from these results?

The results have shown a consistent pattern at the comparison of loads with conventional vertical walls, and evaluation of
practical consequences is first based on the assessment of relations between maximum horizontal forces in both directions: $F_{h-ve \ max}/F_{h+ve \ max}$.

From the analysis of this parameter, major differences are raised in the performance referred to in ‘Proverbs’ for vertical breakwaters: in the case of conventional caissons, for relative depths $h_s/L < 0.25$, negative (net seaward) forces may be higher than positive (net landward) forces for most wave steepnesses; for small relative wave heights ($H_s/h_s < 0.3$), there is a small possibility that negative forces may exceed positive forces ($F_{h-ve \ max}/F_{h+ve \ max} > 1$). While this situation occurs for the majority of the cases, in deeper water conditions, $H_s/h_s < 0.2$.

However, that pattern does not occur for this perforated type of caisson, where positive forces are greater than seaward forces in almost all cases tested (Figure 9), regardless of the value of the $H/h_s$ parameter.

Viewing the results in terms of reduction in forces and moments compared with a conventional caisson, the capacity of the structure to resist sliding needs to be evaluated, since the dead weight of this type of caisson is also much smaller. For example, for a 49 m long caisson of this new type, the resulting dead weight is slightly $> 19,000$ t (including reinforced concrete and fill inside the cylinders). In addition, the dead weight of the crown wall is close to 3250 t, so it results in a dead weight of some 22,350 t and some 455 t/m. This means a significant reduction in stabilising loads compared with a conventional massive caisson (with a total dead weight of some

<table>
<thead>
<tr>
<th>$H$: m</th>
<th>$T$: s</th>
<th>Maximum horizontal wave forces: %</th>
<th>Maximum moments: %</th>
</tr>
</thead>
<tbody>
<tr>
<td>6.0</td>
<td>7.5</td>
<td>56</td>
<td>75</td>
</tr>
<tr>
<td>7.5</td>
<td>8.5</td>
<td>52</td>
<td>80</td>
</tr>
<tr>
<td>9.0</td>
<td>9.5</td>
<td>60</td>
<td>86</td>
</tr>
<tr>
<td>10.0</td>
<td>11.5</td>
<td>55</td>
<td>86</td>
</tr>
<tr>
<td>11.5</td>
<td>12.5</td>
<td>63</td>
<td>86</td>
</tr>
</tbody>
</table>

Table 2. Reduction (%) of maximum horizontal forces and moments on the structure

<table>
<thead>
<tr>
<th>$H$: m</th>
<th>$T$: s</th>
<th>Maximum seaward horizontal wave forces: %</th>
<th>Maximum seaward moments: %</th>
</tr>
</thead>
<tbody>
<tr>
<td>6.0</td>
<td>7.5</td>
<td>74</td>
<td>79</td>
</tr>
<tr>
<td>7.5</td>
<td>8.5</td>
<td>64</td>
<td>74</td>
</tr>
<tr>
<td>9.0</td>
<td>9.5</td>
<td>62</td>
<td>70</td>
</tr>
<tr>
<td>10.0</td>
<td>11.5</td>
<td>63</td>
<td>71</td>
</tr>
<tr>
<td>11.5</td>
<td>12.5</td>
<td>50</td>
<td>76</td>
</tr>
</tbody>
</table>

Table 3. Reduction (%) of maximum seaward forces and moments on the structure
56 000 t during service life, including all the elements) and therefore sliding resistance evaluation is needed initially to validate the viability of this solution.

The Spanish Recomendaciones Geotécnicas para Obras Marítimas y Portuarias (ROM) standard (Puertos del Estado, 2005) establishes the sliding evaluation according to the resulting sliding safety factor ($F_{\text{slid}}$), defined as

$$F_{\text{slid}} = \frac{\mu \sum V}{\sum H}$$

where $\mu$ denotes the coefficient of static friction between the caisson and the embankment, with $\mu = \tan(\Phi_c)$ and $\Phi_c$ being the internal friction angle within the contact surface. In addition, in Equation 5 $\sum V$ and $\sum H$ represent the total vertical and horizontal design loads (i.e. the characteristic values have been multiplied by their relevant partial load factor $\gamma$).

According to the maximum wave loads recorded during the tests and assuming $\mu = \tan(32^\circ) = 0.62$, the sliding safety factor for this new type of caisson results in $F_{\text{slid}} = 1.41$ (greater than the minimum prescribed by ROM standard, which is 1.30). In addition, for the characteristic values of the loads, $\sum H/\sum V = 0.25 < 0.40$, which is another usual requirement in other standards for sliding resistance evaluation in gravity base foundations.

Finally, in the initial calculations, an analytical estimation of maximum bearing pressures transmitted to the foundation ($\sigma$) is included below, in order to validate whether this breakwater type actually represents a major reduction in this regard, both for wave direction (+ve) and seaward (−ve) direction.

<table>
<thead>
<tr>
<th>$H/h$</th>
<th>+ ve: %</th>
<th>− ve: %</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.27</td>
<td>37</td>
<td>44</td>
</tr>
<tr>
<td>0.34</td>
<td>42</td>
<td>45</td>
</tr>
<tr>
<td>0.41</td>
<td>50</td>
<td>45</td>
</tr>
<tr>
<td>0.45</td>
<td>54</td>
<td>48</td>
</tr>
<tr>
<td>0.52</td>
<td>58</td>
<td>53</td>
</tr>
</tbody>
</table>

Table 4. Reduction (%) of maximum bearing pressures ($\sigma$) transmitted to the foundation

A summary of the comparison with respect to a vertical breakwater solution is included in Table 4 and Figure 10. The results are shown with reference to the dimensionless...
parameter $H/h$. Similarly to the sliding evaluation, all the loads are included in the calculation of bearing pressure, not just the contribution of wave actions.

To conclude, the reductions in wave loads on the structure lead to significant reductions of pressures transmitted to the foundation, while this fact does not undermine the capacity of the structure to resist sliding.

The results are consistent and show a regular pattern in terms of horizontal wave forces, moments and loads transmitted to foundations, both for positive and seaward directions.

5. What are the proper tools to predict the performance of this new type of caisson?

The obvious difference of this new type of caisson leads to substantial deviations of loads compared with vertical breakwaters. Related to cylindrical geometries, Morison et al. (1950) established the calculation model of wave forces on isolated cylinders. This formula and all of the models derived from the work of Morison et al. (1950) – Chakrabarti (1994, 2005), Keulegan and Carpenter (1958), Ochi and Tsai (1984), Sarpkaya (1976) and Sarpkaya and Isaacson (1981) – are applicable to isolated vertical cylinders or groups of cylinders, but they do not deal with the case of a breakwater with a chamber. So they seem not to be directly applicable to predict total wave forces on this new type of breakwater and thus, a new parametric experimental approach is needed. However, they need to be taken into account to assess some potential scale effects, as discussed later.

For studies in specific locations, preliminary analysis must be carried out in terms of a set of governing parameters but also based on constructability constraints. The final design should be validated through physical model tests. Nevertheless, this study has led to a number of preliminary conclusions that are useful for potential applications of this breakwater type.

The first point is the definition of the domain in which the tests were carried out, in terms of three key parameters: the coefficient of cylinder density ($\Phi$), the relative wave height ($H/h$) and the relative chamber width ($B/L$).

For these tests $\Phi$ ranged from 0·64 to 0·71. According to Akilly et al. (2004), for $\Phi \leq 0·5$ it may be deemed that the front cylinders no longer interact, leading to a significant increase of the incident energy in the rear wall in that situation, losing some of the benefits of the solution. Conversely, high values of $\Phi$ can cause a blockage effect (produced by the mass of water ‘retained’ in front of the caisson), increasing wave loads in the front perforated wall.

Regarding the performance in terms of relative wave height, Figure 11 shows the maximum horizontal loads for this perforated caisson normalised by those from an equivalent conventional caisson previously described, similar to that of Takahashi et al. (1991) for perforated vertical walls. For every case in the present work, $d'/d = 1·00$ and $dh/h = 0·91$. The reductions, in terms of the rate in maximum horizontal wave loads between the present perforated caisson ($F_{inn}$) and conventional vertical wall ($F_{con}$), are larger than those evaluated by Takahashi et al. (1991) for other perforated caisson types. Here it is about 0·40, while this rate in the tests of Takahashi et al. (1991) ranged approximately from 0·80 to 0·60.

The performance tends to be similar for the wide range of $H/h$ values tested, typically from 0·15 to 0·55 (Figure 11).

Additionally, a similar pattern occurs in terms of the dimensionless parameter $B/L$, which ranged approximately from 0·10 to 0·20 in this study (Figure 12).

![Figure 11. Maximum wave force rates between the innovative and conventional vertical wall caissons](image1)

![Figure 12. Maximum wave force rates between the innovative and conventional vertical wall caissons in terms of $B/L$](image2)
In conclusion, when $H_d/h < 0.55$, a rate of $B/L \approx 0.15$ will lead to a reduction in maximum wave forces according to $F_{\text{in}}/F_{\text{conv}} \approx 0.40$. Regarding the comparison in bearing pressures transmitted to foundations with respect to a conventional caisson, results are shown in Table 4 and Figure 10, with larger differences between types as the incident wave height increases. Thus, while in the absence of waves the reduction in pressures transmitted to the foundation is about 25%, the reduction is above 50% for the higher storm waves tested.

Once the ranges of the key parameters have been defined, the next step is the identification of the variables that may govern total positive wave forces. One principal variable has been detected for this purpose: the incident wave energy per unit length ($E'$), described as

$$ E' = \frac{\rho g}{2} \left( \frac{H}{2} \right)^2 L $$

In a formal way, $E'$ is expressed in kJ/m when $\rho g$ is entered in kN/m$^3$. Furthermore, the second expression in Equation 6 can also express a force in kN, and be used as a descriptive variable of the wave forces against the cylinders.

To be scaled with the width of the structure and obtain the forces per unit length, the second expression in Equation 6 needs to be affected by a factor $1/D_{\text{front}}$ ($D_{\text{front}}$ being the diameter of the front cylinders). In addition, the wave energy term needs to be affected by another correction factor which, in turn, depends on two dimensionless variables: $H_i/h$ and $B/L$. These factors have exponential adjustments according to the test results. So the resulting model shows a predictive performance as shown in Figure 13, which conforms to a model as follows

$$ F_{\text{calc}} (\text{kN/m}) = a \frac{1}{D_{\text{front}}} \frac{\rho g}{2} \left( \frac{H_i}{2} \right)^2 L e^{b (H_i/h + c B/L)} $$

The values of $a$, $b$ and $c$ factors depend on the configuration of the tie beam which braces the front cylinders against each other at the top of the caisson. This beam is needed for structural reasons, but its elevation with reference to the water level may be decided by the designer.

As explained previously, three configurations of this front beam were tested. Assuming in Equation 7 that $\rho g = 10.06$ kN/m$^3$, then $a$, $b$ and $c$ factors are as shown in Table 5 according to the test results.

As explained previously, three configurations of this front beam were tested. Assuming in Equation 7 that $\rho g = 10.06$ kN/m$^3$, then $a$, $b$ and $c$ factors are as shown in Table 5 according to the test results.

Nevertheless, Equation 7 shows a similar performance for the three cases. Figure 13 shows the results and tendency lines of adjustment for each case when the model is compared with the test results.

The previous model can be used for predesign purposes in cases where $\Phi$ (or the porosity) of the front wall is within the range of these tests.

Finally, the analysis for irregular waves would remain homogeneous with the aforementioned Equation 7, simply by using
Elevation of the front tie beam*  a  b  c
- 6:00  1:26  -3:77  -1:41
+ 3:00  1:43  -3:90  -1:47
No tie beam  12:94  -6:81  -10:88

*Still water level at ±0·00 m

Table 5. Factors a, b and c as a function of the configuration of the front tie beam at the top of the cylinders

\( H_d = \min(H_l, H_b) \) instead of \( H_v \). However, in that case, values of factors a, b and c would need to be evaluated again.

6. Discussion of potential scale effects

Pressure law distribution (and therefore resulting forces) along a vertical slender cylinder subjected to a steady flow depends on the Reynolds number (Re), defined as

\[ Re = \frac{UD}{v} \]

where \( U \) is the horizontal wave velocity, \( D \) is the cylinder diameter and \( v \) is the kinematic viscosity of water. So due to the application of Froude’s similarity, there exists a distortion in the Re between the model and the prototype.

Furthermore, the problem requires the definition of the inertia and drag coefficients (\( C_M \) and \( C_d \)) both for the model and the prototype, since these coefficients affect the estimation of inertia and drag forces. Thus the problem consists of the estimation of \( C_{d\text{mod}}/C_{d\text{prot}} \) and \( C_{d\text{mod}}/C_{d\text{prot}} \). However, complexity increases as the structure itself leads to an increase in wave height in front of the caisson, which also affects the values of \( C_M \) and \( C_d \). Furthermore, \( C_d \) and \( C_M \) show high variability in the vicinity of \( Re \sim 10^5 \), which is the case of the authors’ model.

In addition, there are several curves of \( C_d \) against \( Re \) as a function of the Keulegan–Carpenter number (KC, which is the rate between the orbital amplitude of the wave and the diameter of the cylinder), which were described by Sarpkaya (1976). Chakrabarti (1994) developed guidance on how \( C_d \) should be modified according to \( \Phi \) variations for different values of \( Re \) owing to the blockage effect due to the presence of the structure. Finally, the use of relative roughness concept (\( K \)), as it was defined by Nikuradse (1933), must be adapted to the authors’ problem.

On the basis of what is mentioned above, the discussion of these scale effects is included at the end of the paper as an Appendix. In conclusion, relative roughness factor (\( K \)) and the variability of \( C_d \) with \( \Phi \) stand as the most influential variables in the estimation of potential scale effects, in those cases where drag forces become increasingly relevant. So it is advisable to perform specific physical tests for each particular project in which similar caissons are adopted, specifically tests with large ranges of \( \Phi \) and roughness.

The use of freshwater in the tests is another issue to be assessed regarding the potential scale effects, due to the difference in density and also due to the fact that air behaves differently in the model than in seawater. The latter effect is related to water aeration affecting the results in peak pressure values. Bullock et al. (2000) in the University of Plymouth have shown that the freshwater peak pressure values were about 10% higher than those for seawater. However, when the rise time of an impulse was taken into account, the impulse, or the impulsive loading, on the model breakwater was of the same order. So these scale effects do not seem to alter the tests’ key conclusions significantly.

7. Potential adaptations to key construction constraints

The caisson is designed to be built using the floating dock construction technique (Figure 14) – that is, with the use of sliding formworks – and it has been designed to be towed and installed taking advantage of its own buoyancy conditions.

The main constraint for the construction viability is the available draught at the construction quay. The bottom slab can be continuous or not (as it is in the model tested). The former involves higher stability during buoyancy stages (towing and installation) but a larger draught is needed during fabrication. The latter slab configuration may be preferable for the following reasons.

- There is sufficient safety margin for buoyancy stability if the caisson is wide enough. Buoyancy stability is evaluated in terms of metacentric height (GM) and it is usually required to be larger than 0:50 m (higher values can be required for some marine operations in non-sheltered areas).
- The previous requirement involves caisson widths compatible with current floating docks’ capacities and also values of \( BL \) near the optimum for standard storm wave conditions.
- The dynamic uplift pressure decreases as the porosity of the bottom slab increases. In the model tested, the bottom slab is simply formed by the bottom of the cylinders (Figure 1). However, the beams at the bottom that brace one cylinder against the cylinder of the opposite wall may be modified in order to be part of the bottom slab as well.
In the case of a continuous bottom slab, uplift pressures may be relevant to stability evaluation due to the reduced weight of the caisson. In that case, it would be necessary to conform cells to be filled up to some level in order to gain enough weight, similar to conventional gravity caissons; and thus, the lower part of the shaft would be closed through the perimeter of the caisson (i.e. with connection walls between adjacent cylinders up to some level). In this case, the $d'/d$ parameter would change from the current test conditions, where $d'/d = 1.00$, and the wave loads could change accordingly.

In case of strong constraints in existing draughts in the construction quay, it could also be possible to use the pontoon of the floating dock’s own buoyancy until caisson launching, towing the floating dock–caisson assembly to a place with higher water depths.

The tie beams and their joints to cylinders can be built within the floating dock as well, provided that beams have regular cross-sections.

Regarding installation, the caisson can be installed onto the embankment by ballasting the cylinders with seawater while the final sand ballast can be pumped hydraulically by suction dredgers or poured from trucks and loaders from the top of the caisson using temporary and movable working platforms. In the case of hydraulic filling by dredgers, the pore pressure of the filling might be too high during the start of the process. So the dredgers should pump at low flow rates, in order to adapt the filling to the internal pore pressure dissipation process. Otherwise, the cylinders’ wall should be thicker for structural reasons, leading to major implications in floating conditions during the construction phase.

8. Conclusions

Test results for this type of caisson demonstrate a substantial improvement in load transmission to foundations. First, the reductions in maximum wave loads are larger than other non-conventional types based on perforated vertical walls. Second, there is a significant reduction of dead weight of the structure compared with a conventional gravity caisson.

The wave load results for the new type show a regular pattern when compared with conventional vertical wall breakwaters. In addition, the analysis can be simplified due to the fact that positive wave forces (seaward) are greater than negative ones for almost every value of $H/h$, which is another significant difference compared with conventional caissons.

As an initial approach to addressing the hydrodynamic complexity of the system, it is recommended to set a first range of geometrical parameters near the optimum regarding wave load reduction, according to the aforementioned reference tests for perforated caissons with a single chamber. Primarily the proposed parameters are the cylinder density parameter ($\Phi$) and $B/L$. For breakwaters with this new type of caisson, the authors recommend adopting values of $\Phi$ in the range of 0.65–0.70 and $B/L$ in the vicinity of 0.15, since these values also solve major construction constraints.

A new predictive model for maximum total wave loads has been proposed here as a function of incident wave energy, $B/L$ and $H/h$. 
Moreover, the possible effects of scale derive from the tests have been identified, analysed and estimated, concluding that the roughness of the cylinders is a key issue that could affect the validity of test results.

Finally, hydraulic performance allows further modifications in order to make the new type of caisson more adaptable to construction procedure constraints, while it has been designed to be built with the current floating dock facilities.

9. Future research

Testing under random waves and with potential impulsive load conditions would be the scope of further works. In addition, the response to oblique waves may alter some of the conditions that help in the design of breakwaters. Likewise, there remains a field of research in terms of a wider range of values of the Φ parameter, BiL and H/h for plunging breaker conditions. However these situations may involve an increase of B (and therefore the caisson width) that exceeds the capacity of the conventional construction techniques with floating docks. In addition, these increases in the construction width could lead to a departure from the optimum values of BiL in accordance with the existing reference works.

Additionally, there could be some design adaptations to obtain better buoyancy and reduce the draught required at the construction quay, which might be a major constraint in some locations. This would imply some differences in the hydraulic performance of the caisson during service life.

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Appendix: Discussion of potential scale effects

A1.1 The influence of Re and drag forces

The pressure distribution along a vertical cylinder subjected to an oscillatory flow has two terms. The first is related to the stationary flow and it is proportional to $U^2(t)$, with $U(t)$ being the horizontal particle speed, while the second is an inertial term and is proportional to flow acceleration $dU(t)/dt$.

According to Morison et al. (1950), the first term can be described as a drag force as follows

$$dF_d = C_d(Re)\rho D \frac{U^2}{2}$$

where $C_d$ is the drag coefficient and depends on the Re. On the other hand, the second term can be described as

$$dF_i = C_M \frac{\pi D^2 \frac{dU(t)}{dt}}{4}$$

where $C_M \approx 2$ for a smooth cylinder and continuous potential flow.

The Re represents the rate between mass and viscosity forces and can be defined as follows for a vertical slender cylinder subjected to a steady flow

$$Re = \frac{UD}{v}$$

where D is the cylinder diameter and v is the kinematic viscosity of water.

Owing to the application of Froude’s similarity, there exists a distortion in the Re between the model and the prototype. From the dimensional analysis it can be stated as follows

$$Re = \frac{F_{mass}}{F_{visc}} = \frac{\rho v^2 L^2}{\nu L v} = \frac{v L \rho}{v}$$

where $\rho$ is the density, v the velocity, L the length and $\nu$ is the viscosity.

The application of Froude’s similarity (Froude number, $F_{Fr}$, is the relation between mass and inertia forces) implies that

$$\frac{F_{Fr, model}}{F_{Fr, protot}} = 1 \Rightarrow \frac{n_{Fr}}{n_{Fr}} = \frac{n_{(\rho/v)_{model}}}{n_{(\rho/v)_{protot}}} = 1 \Rightarrow n_{t}^2 = n_L$$

which verifies the cinematic similarity condition.

Furthermore, assuming Froude similarity, $(\rho/v)_{model}/(\rho/v)_{protot} = 1$ and being the chosen scale $n_L = n_{model}/n_{protot} = 1/\lambda$, then the
proportionality between Re in the model and the prototype is

\[ \frac{R_{em}}{R_{ep}} = \left( \frac{1}{\lambda} \right)^{3/2} \Rightarrow R_{ep} = \lambda^{3/2} R_{em} \]

Since the scale used was 1:25 (i.e. \( \lambda = 25 \)), the Re in the model is around 125 times smaller than in the prototype. In fact the model is in \( O(10^3) \) while the prototype is in \( O(10^5) \). That is, the tests should have used a fluid with kinematic viscosity 125 times smaller in order to keep proportionality in viscous forces with the prototype. So there is a distortion in the value of \( C_d \) and it is needed to assess how the proportion in drag forces have been distorted in the estimation of total wave forces.

Furthermore, \( C_d \) and \( C_M \) show high variability in the vicinity of \( Re \sim 10^5 \), which is the case of the authors’ model. Indeed, a flow passing around a smooth cylinder shows different values of \( C_d \) as a function of Re, with a sudden variation in the vicinity of Re, \( \sim 10^5 \); where a turbulent boundary layer separation occurs: the boundary layer partly remains laminar and partly becomes turbulent as well as the wake downstream of the cylinder (sudden transition between subcritical and supercritical zone). This phenomenon was studied by several authors, both from laboratories and in field studies, mostly from the 1950’s onwards, with conclusions and results summarised in, amongst others, the Shore Protection Manual (USACE, 1984).

So any approach to the problem should be based on estimations of \( C_{dp}^{mod}/C_{dp}^{prot} \) and \( C_{M}^{prot}/C_{M}^{mod} \).

In addition, variations of \( C_M \) and \( C_d \) with Re are also dependent on the KC, which is the rate between the orbital amplitude of the wave and the diameter of the cylinder

\[ KC = \frac{A}{D} = \frac{u_{\text{max}} T}{D} \]

where \( A \) is the orbital amplitude of the wave movement, \( D \) is the diameter of the cylinder, \( u_{\text{max}} \) is the maximum horizontal wave velocity and \( T \) is the wave period.

These curves were described by Sarpkaya (1976) according to the frequency parameter \( \beta \).

16. \[ \beta = \frac{Re}{KC} \]

In the authors’ case, KC is in the range 15–20 both in the model and the prototype. \( C_M \) is almost constant \((C_M \approx 2.0)\) if \( \beta > 6000 \), as it is in the model; whereas there is high variability as \( \beta \) decreases, as occurs at prototype scale. Plus, \( \beta \) curves by Sarpkaya (1976) show different shapes and high influence in \( C_d \) estimation.

Furthermore, if roughness is not modelled properly, the model and the prototype move through different \( C_d \) against Re curves. The relative roughness concept \((K)\), as it was defined by Nikuradse (1933), is defined as follows

\[ K = \frac{k_s}{D} \]

where \( k_s \) is the equivalent sand diameter. The curves were also described by Sarpkaya (1976).

The influence of \( k_s/D \) in \( C_d \) can be relevant in this problem, for example, when taking into consideration the effect of marine growth in the cylinders.

Additional issues arise from the fact that the structure itself leads to an increase of wave height in front of the caisson, which also affects \( C_M \) and \( C_d \) coefficients. Chakrabarti (1994) developed guidance on how \( C_d \) should be modified according to \( \Phi \) variations due to the blockage effect owing to the presence of several cylinders side by side. In that case, \( C_d \) can be called \( C_e \) (effective drag coefficient) and changes with Reynolds number also, with different curves depending on whether Re is greater or lower than \( 4.2 \times 10^5 \).

This blockage effect needs to be assessed when the analysis comes from individual cylinders. However, this effect is already reproduced during physical tests. Anyway \( C_e \) variation with \( \Phi \) shows different patterns as a function of Re.

To sum up, the key conclusions from the scale effect discussion are as follows.

- Assessment of Re number distortion is highly complex for this typology, since it depends on the horizontal wave velocity and acceleration. So it is variable both in time and in depth along the cylinders. In addition, analysis from individual cylinders subjected to steady flows are not completely applicable, since the caisson has a chamber and the maximum wave forces to the caisson do not occur at the same time as the maximum forces in the front cylinders, neither does this necessarily occur with \( H_{\text{max}} \) in the case of irregular waves. Thus, tests with regular waves seem to be a good approach for a first estimation of these scale effects.

- The distortion in the Re between the model and the prototype implies a variation in \( C_d \). For a single cylinder, the value of the Re number in the prototype is \( O(10^5) \) but
Higher levels of aeration of seawater produce a greater cushioning effect that reduces the dynamic peak pressures over the structure. It is reasonable to accept that the main difference between freshwater and seawater pressure values is the different levels of aeration within these fluids.

The pressure variation during a wave impact will change the volume of the entrained air and will change the voids ratio.

Laboratory tests with freshwater and seawater conducted by Bullock et al. (2000) in the University of Plymouth have shown that freshwater peak pressure values were about 10% higher than those for seawater. However, when rise time was taken into account, the impulse, or the impulsive loading, on the model breakwater was of the same order.

As a conclusion, the authors can state that entrained air might reduce maximum impact pressures and increase rise times. Moreover, freshwater tests considering Froude law lead to a likely overestimation of 10% in impact pressures. Scale effects do not seem to alter significantly the tests’ key conclusions and therefore they can be taken as valid.

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